

AN INTERVIEW WITH F. WILLIAM LAWVERE - PART TWO

You studied in Columbia from February 1960 to June 1961, returning there for the Ph.D. defense in May 1963. In the interim you went to Berkeley and Los Angeles. Why?

Even though I had had an excellent course in mathematical logic from Elliott Mendelson at Columbia, I felt a strong need to learn more set theory and logic from experts in that field, still of course with the aim of clarifying the foundations of category theory and of physics. In order to support my family, and also because of my deep interest in mathematics teaching, I had taken up employment over the summers of 1960 and 1961 with TEMAC, a branch of the Encyclopedia Britannica, which was engaged in producing high school text books in modern mathematics in a new step-wise interactive format. In 1961, TEMAC built a new building near the Stanford University campus devoted to that project. Thus the further move was not due to having lost a grant, but rather for those two purposes: in the Bay area I could reside in Berkeley, follow courses by Tarski, Feferman, Scott, Vaught, and other leading set theorists, and also commute to Palo Alto to process the text book which I was writing mainly at home. Nor was my first destination in California the think tank referred to in Mac Lane's book. Rather, since my slow progress in writing my second programmed textbook was not up to the speed which I thought TEMAC expected, I resigned from that job. A friend from the Indiana days now worked for the think tank near Los Angeles, and was able to persuade them to give me a job. At the beginning I understood that the job would involve design of computer systems for verifying possible arms control agreements; but when I finally got the necessary secret clearance, I discovered that other matters were involved, related with the Vietnam war. Mac Lane's account is essentially correct concerning the way in which my friend and fellow mathematician Bishop Spangler in the think tank became my supervisor and then gave me the opportunity to finish my thesis on categorical universal algebra. In February 1963, wanting very much to get out of my Los Angeles job to take up a teaching position at Reed College, I asked Eilenberg for a letter of recommendation. His very brief reply was that the request from Reed would go into his waste basket unless my series of abstracts be terminated post haste and replaced by an actual thesis. This tough love had the desired effect within a few weeks.

Having defended the Ph.D. in May 1963, I was able to leave the think tank and re-enter normal life as an

assistant professor at Reed College for the academic year 1963-64. En route to Portland I attended the 1963 Model Theory meeting in Berkeley, where besides presenting my functorial development of general algebra, I announced that quantifiers are characterized as adjoints to substitution.

So, you spent the academic year 1963-64 as an assistant professor at Reed College.

At Reed I was instructed that the first year of calculus should concentrate on foundations, formulas there being taught in the second year. Therefore, in spite of already having decided that the category of categories is the appropriate framework for mathematics in general, I spent several preparatory weeks trying to devise a calculus course based on Zermelo-Fraenkel set theory. However, a sober assessment showed that there are far too many layers of definitions, concealing differentiation and integration from the cumulative hierarchy, to be able to get through those layers in a year. The category structure of Cantor's structureless sets seemed both simpler and closer. Thus, the Elementary Theory of the Category of Sets arose from a purely practical educational need, in a sort of experience that Saunders also noted: the need to explain daily for students is often the source of new mathematical discoveries.

A theory of a category of Cantorian abstract sets has the same proof-theoretic strength as the theory of a Category of Categories that I had initiated in the Introduction to my thesis. More objectively, sets can be defined as discrete categories and conversely categories can be defined as suitable finite diagrams of discrete sets, and the relative strengths thus compared. The category of categories is to be preferred for the practical reason that all mathematical structures can be constructed as functors and in the proper setting there is no need to verify in every instance that one has a functor or natural transformation.

After Reed I spent the summer of 1964 in Chicago, where I reasoned that Grothendieck's theory of Abelian categories should have a non-linear analogue whose examples would include categories of sheaves of sets; I wrote down some of the properties that such categories should have and noted that, on the basis of my work on the category of sets, such a theory would have a greater autonomy than the Abelian one could have (it was only in the summer of 1965 on the beach of La Jolla that I learned from Verdier that he, Grothendieck

and Giraud had developed a full-blown theory of such “toposes”, but without the autonomy). Later, at the ETH in Zurich ...

... where you stayed from September 1964 through December 1966 as visiting research scientist at Beno Eckmann’s *Forschungsinstitut für Mathematik* ...

... there I was able to further simplify the list of axioms for the category of sets in a paper that Mac Lane then communicated to the *Proceedings of the National Academy of Sciences USA*. There I also wrote up for publication the talk on “the category of categories as a foundation for mathematics” which I gave at the first international meeting on category theory at La Jolla, California, 1965.



A. Kock and F. W. Lawvere in Cafe Odeon, Zurich
(Fall of 1966; photo courtesy of A. Kock).

Which were the purposes of your elementary theory of the category of sets?

It was intended to accomplish two purposes. First, the theory characterizes the category of sets and mappings as an abstract category in the sense that any model for the axioms that satisfies the additional non-elementary axiom of completeness, in the usual sense of category theory, can be proved to be equivalent to the category of sets. Second, the theory provides a foundation for mathematics that is quite different from the usual set theories in the sense that much of number theory, elementary analysis, and algebra can apparently be developed within it even though no relation with the usual properties of \in can be defined.

Philosophically, it may be said that these developments supported the thesis that even in set theory and elementary mathematics it was also true as has long been felt in advanced algebra and topology, namely that the substance of mathematics resides not in Substance, as

⁷Saunders Mac Lane, *A Mathematical Autobiography*, A K Peters, 2005.

it is made to seem when \in is the irreducible predicate, but in Form, as is clear when the guiding notion is isomorphism-invariant structure, as defined, for example, by universal mapping properties. As in algebra and topology, here again the concrete technical machinery for the precise expression and efficient handling of these ideas is provided by the Eilenberg-Mac Lane theory of categories, functors and natural transformations.

Let us return to Zurich.

At Zurich I had many discussions with Jon Beck and we collaborated on doctrines. The word “doctrine” itself is entirely due to him and signifies something which is like a theory, except appropriate to be interpreted in the category of categories, rather than, for example, in the category of sets. The “algebras” for a doctrine deserve to be called “theories” because dualizing into a fixed algebra defines a semantics functor relating abstract generals and corresponding concrete generals. Jon was insistent on mathematical clarity and did much to encourage precision in discussions and in the formulation of mathematical results. He noted that my structure functor adjoint to semantics is analogous to Grothendieck’s cocycle definition of descent in that both partially express the structure that inevitably arises when objects are constructed by a functorial process, and which if hypothesized helps to reverse the process and discern the origin. Implementing this general philosophical notion of descent requires the choice of an appropriate “doctrine” of theories in which the induced structure can be expressed.

Also from Zurich I attended a seminar in Oberwolfach where I met Peter Gabriel and learned from him many aspects not widely known even now of the Grothendieck approach to geometry. In general the working atmosphere at the *Forschungsinstitut* was so agreeable, that I later returned during the academic year 1968/69.

As an assistant professor in Chicago, in 1967, you taught with Mac Lane a course on Mechanics, where “you started to think about the justification of older intuitive methods in geometry”⁷. You called it “synthetic differential geometry”. How did you arrive at the program of Categorical Dynamics and Synthetic Differential Geometry?

From January 1967 to August 1967 I was Assistant Professor at the University of Chicago. Mac Lane and I soon organized to teach a joint course based on Mackey’s book “Mathematical Foundations of Quantum Mechanics”.

So, Mackey, a functional analyst from Harvard mainly concerned with the relationship between quantum me-

chanics and representation theory, had some relation to category theory.

His relation to category theory goes back much further than that, as Saunders and Sammy had explained to me. Mackey's Ph.D. thesis displayed remarkable thinking of a categorical nature, even before categories had been defined. Specifically, the fact that the category of Banach spaces and continuous linear maps is fully embedded into a category of pairings of abstract vector spaces, together with the definition and use of "Mackey convergence" of a sequence in a "bornological" vector space were discovered there and have played a basic role in some form in nearly every book on functional analysis since. What is perhaps unfortunately not clarified in nearly every book on functional analysis, is that these concepts are intensively categorical in character and that further enlightenment would result if they were so clarified.

And the referee who, despite initial skepticism, permitted the first paper giving an exposition of the theory of categories to see the light of day in the TAMS in 1945, was none other than George Whitelaw Mackey.

Back to the origins of Synthetic Differential Geometry, where did the idea of organizing such a joint course on Mechanics originate?

Apparently, Chandra had suggested that Saunders give some courses relevant to physics, and our joint course was the first of a sequence. Eventually Mac Lane gave a talk about the Hamilton-Jacobi equation at the Naval Academy in summer 1970 that was published in the *American Mathematical Monthly*.

In my separate advanced lecture series, which was attended by my then student Anders Kock, as well as by Mac Lane, Jean Bénabou, Eduardo Dubuc, Robert Knighten, and Ulrich Seip, I began to apply the Grothendieck topos theory that I had learned from Gabriel to the problem of simplified foundations of continuum mechanics as it had been inspired by Truesdell's teachings, Noll's axiomatizations, and by my 1958 efforts to render categorical the subject of topological dynamics.

Beyond what I had learned from Gabriel at Oberwolfach on algebraic geometry as a gros topos, my particular contribution was to elevate certain ingredients, such as the representing object for the tangent bundle functor, to the level of axioms so as to permit development unencumbered by particular construction. That particular ingredient had apparently never been previously noted in the C -infinity category. It was immediately clear that the program would require development, in a similar axiomatic spirit, of the topos theory of which I had heard in 1965 from Verdier on the beach at La Jolla. Indeed, my appointment at Chicago had been

encouraged also by Marshall Stone who was enthusiastic about my 1966 observation that the topos theory would make mathematical both the Boolean-valued models in general and the independence of the continuum hypothesis in particular. That these apparently totally different toposes, involving infinitesimal motion and advanced logic, could be part of the same simple axiomatic theory, was a promise in my 1967 Chicago course. It only became reality after my second stay at the *Forschungsinstitut* in Zurich, Switzerland 1968-69 during which I discovered the nature of the power set functor in toposes as a result of investigating the problem of expressing in elementary terms the operation of forming the associated sheaf, and after 1969-1970 at Dalhousie University in Halifax, Nova Scotia, Canada, through my collaboration with Myles Tierney.

You went to Dalhousie in 1969 with one of the first Killam professorships.

Indeed, and was able to have a dozen collaborators at my discretion, also supported by Killam.

And then you arrived, together with the algebraic topologist Myles Tierney, to the concept of elementary topos. Could you describe us that collaboration with Myles Tierney?

Myles presented a weekly seminar in which the current stage of the work was described and indeed some of the work was in the form of discussions in the seminar itself: remarks by students like Michel Thiebaud and Radu Diaconescu were sometimes key steps.



Myles Tierney and Dana Scott
(1971 Conference at Dalhousie, photo courtesy of Robert Paré).

Although I had been able to convince myself in Zurich, Rome, and Oberwolfach, that a finite axiomatization was possible, it required several steps of successive simplification to arrive at the few axioms known now. The criterion of sufficiency was that by extending any given

category satisfying the axioms, it should be possible to build others by presheaf and sheaf methods. The “fundamental theorem” of slices, followed by our discovery that left exact comonads also yield toposes, more than covered the presheaf aspect. The concept of sheaves led to the conjecture that subtoposes would be precisely parametrized by certain endomaps of the subobject classifier, and this was verified; those endomaps are now known as Lawvere-Tierney modal operators, and correspond classically to Grothendieck topologies. That the corresponding subcategory of sheaves can be described in finite terms is a key technical feature, which was achieved by making explicit the partial-map classifier. That the theory is elementary means that it has countable models and other features making it applicable to independence results in set theory and to higher recursion, etc, but on the other hand Grothendieck’s theory of U -toposes is precisely included through his own technique of relativization together with additional axioms, such as the splitting of epimorphisms and 2-valuedness, on U itself.

(By the way, those two additional axioms are positive – or geometrical – so that there is a classifying topos for models of them, a fact still awaiting exploitation by set theory.)



Fred Linton and F. William Lawvere (photo courtesy of Robert Paré).

In 1971, official date of the birth of topos theory, unfortunately the dream team at Dalhousie was dispersed. What happened, that made you go to Denmark?

Some members of the team, including myself, became active against the Vietnam war and later against the War Measures Act proclaimed by Trudeau. That Act, similar in many ways to the Patriot Act 35 years later in the US, suspended civil liberties under the pretext of a terrorist danger. (The alleged danger at the time was

a Quebec group later revealed to be infiltrated by the RCMP, the Canadian secret police.) Twelve communist bookstores in Quebec (unrelated to the terrorists) were burned down by police; several political activists from various groups across Canada were incarcerated in mental hospitals, etc. etc. I publicly opposed the consolidation of this fascist law, both in the university senate and in public demonstrations. The administration of the university declared me guilty of “disruption of academic activities”. Rumors began to be circulated, for example, that my categorical arrow diagrams were actually plans for attacking the administration building. My contract was not renewed.

And after a short period in Aarhus, you went to Italy. Why?

Conditions in the *Matematisk Institut* were very agreeable, and the collaboration with Anders Kock was very fruitful and enjoyable. However when the long northern night set in, it turned out to be bad for my health, so I accepted an invitation from Perugia. I still enjoy visiting Denmark in the summer.

After a few years in Europe, you returned to the United States, for SUNY at Buffalo ...

John Isbell and Jack Duskin were able to persuade the dean that (contrary to the message sent out by one of the Dalhousie deans) I was not a danger and might even be an asset.

In spite of your return to the USA, you kept close ties with the Italian mathematical community. In November 2003 there was a conference in Firenze (“Ramifications of Category Theory”) to celebrate the 40th anniversary of your Ph.D. thesis⁸. Could you summarize the main ideas contained in it?

Details are given in my commentary to the TAC Reprint (these Reprints are an excellent source of other early material on categories). The main point was to present a categorical treatment of the relation between algebraic theories and classes of algebras, incorporating the previous “universal” algebra of Birkhoff and Tarski in a way applicable to specific cases of mathematical interest such as treated in books of Chevalley and of Cartan-Eilenberg. The presentation-free redefinition of both the theories and the classes required explicit attention to the category of categories.

In the Firenze conference there were talks both on mathematics and philosophy. You keep interested in the philosophy of mathematics ...

Yes. Since the most fundamental social purpose of philosophy is to guide education and since mathematics

⁸ *Functorial Semantics of Algebraic Theories*, Reprinted in *Repr. Theory Appl. Categ.* 5 (2004) 1-121 (electronic).

is one of the pillars of education, accordingly philosophers often speculate about mathematics. But a less speculative philosophy based on the actual practice of mathematical theorizing should ultimately become one of the important guides to mathematics education.



Ramifications of Category Theory, 2003
(photo by Andrej Bauer, used with permission).

As Mac Lane wrote in his Autobiography, “The most radical aspect is Lawvere’s notion of using axioms for the category of sets as a foundation of mathematics. This attractive and apposite idea has, as of yet, found little reflection in the community of specialists in mathematical logic, who generally tend to assume that everything started and still starts with sets”. Do you have any explanation for that attitude ?

The past 100 years’ tradition of “foundations as justification” has not helped mathematics very much. In my own education I was fortunate to have two teachers who used the term “foundations” in a common-sense way (rather than in the speculative way of the Bolzano-Frege-Peano-Russell tradition). This way is exemplified by their work in Foundations of Algebraic Topology, published in 1952 by Eilenberg (with Steenrod), and the Mechanical Foundations of Elasticity and Fluid Mechanics, published in the same year by Truesdell. Whenever I used the word “foundation” in my writings over the past forty years, I have explicitly rejected that reactionary use of the term and instead used the definition implicit in the work of Truesdell and Eilenberg. The orientation of these works seemed to be “concentrate the essence of practice and in turn use the result to guide practice”. Namely, an important component of mathematical practice is the careful study of historical and contemporary analysis, geometry, etc. to extract the essential recurring concepts and constructions; making those concepts and constructions (such as homomorphism, functional, adjoint functor, etc.) explicit provides powerful guidance for further unified development of all mathematical subjects, old and new.

Could you expand a little bit on that ?

What is the primary tool for such summing up of the essence of ongoing mathematics? Algebra! Nodal points in the progress of this kind of research occur when, as in the case with the finite number of axioms for the metacategory of categories, all that we know so far can be expressed in a single sort of algebra. I am proud to have participated with Eilenberg, Mac Lane, Freyd, and many others, in bringing about the contemporary awareness of Algebra as Category Theory. Had it not been for the century of excessive attention given to alleged possibility that mathematics is inconsistent, with the accompanying degradation of the F-word, we would still be using it in the sense known to the general public: the search for what is “basic”. We, who supposedly know the explicit algebra of homomorphisms, functionals, etc., are long remiss in our duty to find ways to teach those concepts also in high school calculus.

Having recognized already in the 1960s that there is no such thing as a heaven-given platonic “justification” for mathematics, I tried to give the word “Foundations” more progressive meanings in the spirit of Eilenberg and Truesdell. That is, I have tried to apply the living axiomatic method to making explicit the essential features of a science as it is developing in order to help provide a guide to the use, learning, and more conscious development of the science. A “pure” foundation which forgets this purpose and pursues a speculative “foundation” for its own sake is clearly a NON-foundation.

Foundations are derived from applications by unification and concentration, in other words, by the axiomatic method. Applications are guided by foundations which have been learned through education.

You are saying that there is a dialectical relation between foundations and applications.

Yes. Any set theory worthy of the name permits a definition of mapping, domain, codomain, and composition; it was in terms of those notions that Dedekind and later mathematicians expressed structures of interest. Thus, any model of such a theory gives rise to a category and whatever complicated additional features may have been contemplated by the theory, not only common mathematical properties, but also most interesting “set theoretical” properties, such as the generalized continuum hypothesis, Dedekind finiteness, the existence of inaccessible or Ulam cardinals, etc. depend only on this mere category.

During the past forty years we have become accustomed to the fact that foundations are relative, not absolute. I believe that even greater clarifications of foundations will be achieved by consciously applying a concentration of applications from geometry and analysis, that

is, by pursuing the dialectical relation between foundations and applications.

More recently, you have given algebraic formulations of such distinctions as ‘unity vs. identity’ of opposites, ‘extensive vs. intensive’ variable quantities, ‘spatial vs. quantitative’ categories ...

Yes, showing that through the use of mathematical category theory, such questions lead not to fuzzy speculation, but to concrete mathematical conjectures and results.

It has been one of the characteristics of your work to dig down beneath the foundations of a concept in order to simplify its understanding. Here you are truly a descendant of Samuel Eilenberg, in his “insistence on getting to the bottom of things”. We vividly remember a lecture you presented in Coimbra to our undergraduate students. You have recently published a couple of textbooks⁹. Why do you find it important enough to dedicate a significant amount of your time and effort to it?

Many of my research publications are the result of long study of the two problems: (1) How to effectively teach calculus to freshmen. (2) How to learn, develop, and use physical assumptions in continuum thermomechanics in a way which is rigorous, yet simple.



F. William Lawvere and Stephen Schanuel
(Sydney, 1988; photo courtesy of R. Walters).

In other words, the results themselves can only be building blocks in an answer to the question: “How can we

take concrete, pedagogical steps to narrow the enormous gap in 20th century society between the fact that: (a) everybody must use technology which rests on science, which in turn depends on mathematics; yet (b) only a few have a working acquaintance with basic concepts of modern mathematics such as retractions, fixed-point theorems, morphisms of directed graphs and of dynamical systems, Galilean products, functionals, etc.”

Only armed with such concepts can one hope to respond with confidence to the myriad of methods, results, and claims which in the modern world are associated with mathematics. With Stephen Schanuel I have begun to take up the challenge of that question in our book *Conceptual Mathematics* which reflects the ongoing work of many mathematicians.

What is your opinion on the Wikipedia article about you?

The disinformation in the original version has been largely removed, but much remains in other articles about category theory.

We have recently celebrated Kurt Gödel’s 100th birthday. What do you think about the extra-mathematical publicity around his incompleteness theorem?

In *Diagonal arguments and Cartesian closed categories*¹⁰ we demystified the incompleteness theorem of Gödel and the truth-definition theory of Tarski by showing that both are consequences of some very simple algebra in the Cartesian-closed setting. It was always hard for many to comprehend how Cantor’s mathematical theorem could be re-christened as a “paradox” by Russell and how Gödel’s theorem could be so often declared to be the most significant result of the 20th century. There was always the suspicion among scientists that such extra-mathematical publicity movements concealed an agenda for re-establishing belief as a substitute for science. Now, one hundred years after Gödel’s birth, the organized attempts to harness his great mathematical work to such an agenda have become explicit¹¹.

You have always been concerned in explaining how to describe relevant mathematical settings and facts in a categorical fashion. Is category theory only a language?

No, it is more than a language. It concentrates the essential features of centuries of mathematical experience and thus acts as indispensable guide to further development.

⁹F.W. Lawvere and R. Rosebrugh, *Sets for Mathematics*, Cambridge University Press, Cambridge, 2003; F.W. Lawvere and S. Schanuel, *Conceptual Mathematics. A First Introduction to Categories*, Cambridge University Press, Cambridge, 1997.

¹⁰Reprinted in *Repr. Theory Appl. Categ.* 15 (2006) 1-13 (electronic).

¹¹The controversial John Templeton Foundation, which attempts to inject religion and pseudo-science into scientific practice, was the sponsor of the international conference organized by the Kurt Gödel Society in honour of the celebration of Gödel’s 100th birthday. This foundation is also sponsoring a research fellowship programme organized by the Kurt Gödel Society.

What have been for you the major contributions of category theory to mathematics ?

First, the work of Grothendieck in his Tohoku's paper¹². Nuclear spaces was one of the great inventions of Grothendieck. By the way, Silva worked a lot on these spaces and Grothendieck's 1953 paper on holomorphic functions¹³ was inspired by a 1950 paper of Silva¹⁴.

The concept of adjoint functors, discovered by Kan in the mid 1950's, was also a milestone, rapidly incorporated as a key element in Grothendieck's foundation of algebraic geometry and in the new categorical foundation of logic and set theory.

I may also mention Cartesian closedness, the axiomatization of the category of categories, topos theory ... Cartesian closed categories appeared the first time in my Ph.D. thesis, without using the name. The name appeared first in Kelly and Eilenberg's paper¹⁵. I don't exactly agree with the word "Cartesian". Galileo is the right source, not Descartes.

You are regarded by many people as one of the greatest visionaries of mathematics in the beginning of the twentieth first century. What are your thoughts on the future development of category theory inside mathematics ?

I think that category theory has a role to play in the pursuit of mathematical knowledge. It is important to point out that category theorists are still finding striking new results in spite of all the pessimistic things we heard, even 40 years ago, that there was no future in abstract generalities. We continue to be surprised to

find striking new and powerful general results as well as to find very interesting particular examples.

We have had to fight against the myth of the mainstream which says, for example, that there are cycles during which at one time everybody is working on general concepts, and at another time anybody of consequence is doing only particular examples, whereas in fact serious mathematicians have always been doing both.



F. William Lawvere and Maria Manuel Clementino
(Braga, March 2007).

One should not get drunk on the idea that everything is general. Category theorists should get back to the original goal: applying general results to particularities and to making connections between different areas of mathematics.

Interview by Maria Manuel Clementino and Jorge Picado (University of Coimbra)

Francis William Lawvere (born February 9, 1937 in Muncie, Indiana) is a mathematician well-known for his work in category theory, topos theory, logic, physics and the philosophy of mathematics. He has written more than 60 papers in the subjects of algebraic theories and algebraic categories, topos theory, logic, physics, philosophy, computer science, didactics, history and anthropology, and has three books published (one of them with translations into Italian and Spanish), with three more in preparation at this moment. He also edited three volumes of the Springer series *Lecture Notes in Mathematics* and supervised twelve Ph.D. theses. The electronic series *Reprints in Theory and Applications of Categories* includes reprints of seven of his fundamental articles, with author commentaries, among them his Ph.D. dissertation and his full treatment of the category of sets.

At the 1970 International Congress of Mathematicians in Nice he introduced an algebraic version of topos theory which unified geometry and set theory. Worked out in collaboration with Myles Tierney, this theory has since been developed further by many people, with applications to several fields of mathematics. Two of those fields had previously been introduced by Lawvere: (1) His 1967 Chicago lectures (published 1978) on categorical dynamics had shown how toposes with specified infinitesimal objects can provide a flexible geometric background for models of

¹²A. Grothendieck, Sur quelques points d'algèbre homologique, *Tohoku Math. J.* 9 (1957) 119-121.

¹³A. Grothendieck, Sur certains espaces de fonctions holomorphes, I, *J. Reine Angew. Math.* 192 (1953) 35-64.

¹⁴J. Sebastião e Silva, Analytic functions and functional analysis, *Portugaliae Math.* 9 (1950) 1-130.

¹⁵S. Eilenberg and G. M. Kelly, Closed categories, in: *Proc. Conf. Categorical Algebra* (La Jolla, Calif., 1965), pp. 421-562, Springer, 1966.

continuum physics, which led to a new subject known as Synthetic Differential Geometry; (2) In his 1967 Los Angeles lecture, and his 1968 papers on hyperdoctrines and adjointness in foundations, Lawvere had launched and developed the field of categorical logic, which has since been widely applied to geometry and computer science. Those ideas were indispensable for his 1983 simplified proof of the existence of entropy in non-equilibrium thermomechanics.

Many of Lawvere's research publications result from efforts to improve the teaching of calculus and of engineering thermomechanics. In particular, it was his 1963 Reed College course in the foundations of calculus which led to his 1964 axiomatization of the category of sets and ultimately to the elementary theory of toposes.

Professor Lawvere studied with Clifford Truesdell and Max Zorn at Indiana University and completed his Ph.D. at Columbia in 1963 under the supervision of Samuel Eilenberg. Before completing his Ph.D., Lawvere spent a year in Berkeley as an informal student of model theory and set theory, following lectures by Alfred Tarski and Dana Scott. During 1964-1966 he was a visiting research professor at the *Forschungsinstitut für Mathematik* at the ETH in Zurich. He then taught at the University of Chicago, working with Mac Lane, and at the City University of New York Graduate Center (CUNY), working with Alex Heller. Back in Zurich for 1968-69 he proposed elementary (first-order) axioms for toposes generalizing the concept of the Grothendieck topos. Dalhousie University in 1969 set up a group of Killam-supported researchers with Lawvere at the head; but in 1971 it terminated the group because of Lawvere's political opinions (namely his opposition to the 1970 use of the War Measures Act).

Then Lawvere went to the *Institut for Matematiske* in Aarhus (1971-72) and ran a seminar in Perugia, Italy (1972-1974) where he especially worked on various kinds of enriched category. From 1974 until his retirement in 2000 he was professor of mathematics at the University at Buffalo, often collaborating with Stephen Schanuel. There he held a Martin professorship (1977-82). He was also a visiting research professor at the IHES Paris (1980-81). He is now Professor Emeritus of Mathematics and Adjunct Professor Emeritus of Philosophy at the State University of New York at Buffalo and continues to work on his 50-year quest for a rigorous and flexible framework for the physical ideas of Truesdell and Walter Noll, based on category theory.

His personal view of mathematics and physics, based on a broad and deep knowledge, keeps influencing mathematicians and attracting experts from other areas to Mathematics. This influence was very apparent in the honouring session that took place in the last **International Category Theory Conference** (Carvoeiro, Portugal, June 2007), on the occasion of his 70th Birthday, through spontaneous and intense testimonies of both senior mathematicians and young researchers. Indeed, besides his extraordinary qualities as a mathematician, we wish to stress the care and efforts he puts into the guidance of students and young researchers, which we could confirm in Coimbra when he gave a lecture on Category Theory to undergraduate students, and again in the dialog we were very honoured to be part of, during the preparation of this interview.

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